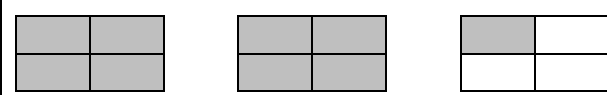


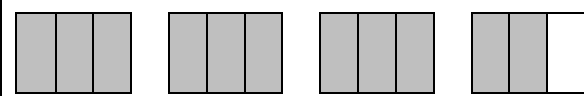
Key Vocabulary	
Proper fraction	A fraction where the numerator is smaller than the denominator e.g. $\frac{2}{3}$
Improper fraction	A fraction where the numerator is bigger than the denominator e.g. $\frac{5}{2}$ Also known as a vulgar or top-heavy fraction
Mixed Number	A whole number and fraction together, e.g. $2\frac{1}{2}$ Improper fractions can be changed to mixed numbers and back again. $\frac{5}{2} = 2\frac{1}{2}$
Equivalent Fractions	Two fractions that represent the same amount. Multiplying or dividing the top and bottom of a fraction by the same number gives an equivalent fraction. Dividing gives a simpler fraction
Percentage	A value out of 100. E.g. $23\% = \frac{23}{100} = 0.23$
Increase	Make a value bigger by a given fraction or percentage
Decrease	Make a value smaller by a given fraction or percentage
Multiplier	A decimal that can be used to multiply a given value to give the result of a percentage increase or decrease

**Key facts / Diagrams**



$2\frac{1}{4} = \frac{9}{4}$   
 $2 \times 4 = 8$        $8 + 1 = 9$   
 Total = 9 quarters =  $\frac{9}{4}$

Change  $\frac{11}{3}$  to a mixed number:  
 $11 \div 3 = 3$  remainder  $2 = 3\frac{2}{3}$



50% =  $\frac{1}{2}$  =  $\div 2$   
 25% =  $\frac{1}{4}$  =  $\div 4$   
 75% =  $\frac{3}{4}$  =  $\div 4$  then  $\times 3$   
 10% =  $\frac{1}{10}$  =  $\div 10$   
 20% =  $\frac{1}{5}$  = either  $\div 5$  or find 10% and  $\times 2$   
 5% =  $\frac{1}{20}$  = either  $\div 20$  or find 10% and  $\div 2$

20% increase = original 100% + 20% = 120%  
 20% decrease = original 100% - 20% = 80%

$\frac{1}{4}$  increase = original +  $\frac{1}{4} = \frac{5}{4}$   
 $\frac{1}{4}$  decrease = original -  $\frac{1}{4} = \frac{3}{4}$

**Common misconceptions**

- You can't have more than 100%. Not realising that while in real life contexts over 100% might not make sense, but through a percentage increase you can have over 100%.
- When asked to multiply a fraction by a whole number, e.g. multiply  $\frac{3}{4}$  by 2, multiplying top and bottom by 2 and just getting an equivalent fraction.  
 Proper method:  $2 \times \frac{3}{4} = \frac{2}{1} \times \frac{3}{4} = \frac{6}{4} = \frac{3}{2} = 1\frac{1}{2}$
- When multiplying two fractions, thinking you need to start by changing them to fractions with the same denominator.

**Worked examples**

Increase £200 by  $\frac{1}{4}$  :  
 Find  $\frac{1}{4}$  of £200 =  $\text{£}200 \div 4 = \text{£}50$   
 $\text{£}200 + \text{£}50 = \text{£}250$   
 OR:  $\text{£}200 \times 5 \div 4 = \text{£}1,000 \div 4 = \text{£}250$   
 OR:  $\text{£}200 \div 4 \times 5 = \text{£}50 \times 5 = \text{£}250$

Decrease £300 by 20%  
 This leaves 80%.  
 Find 10%:  $\text{£}300 \div 10 = \text{£}30$   
 $80\% = \text{£}30 \times 8 = \text{£}240$   
 OR:  $\text{£}300 \times 0.8 = \text{£}240$

Increase 40m by 30%  
 Multiplier = 1.3  
 $40 \times 1.3 = 52\text{m}$